

1. Find the first three terms in the expansion of $(9 - 16x)^{\frac{3}{2}}$ in ascending powers of x , and state the set of values for which this expansion is valid. [5]

2. i. Show that $\frac{x}{(1-x)^3} \approx x + 3x^2 + 6x^3$ for small values of x . [2]

- ii. Use this result, together with a suitable value of x , to obtain a decimal estimate of the value of $\frac{100}{729}$. [4]

- iii. Show that $\frac{x}{(1-x)^3} = -\frac{1}{x^2} \left(1 - \frac{1}{x}\right)^{-3}$. Hence find the first three terms of the binomial expansion of

$$\frac{x}{(1-x)^3} \text{ in powers of } \frac{1}{x}.$$

- iv. Comment on the suitability of substituting the same value of x as used in part (ii) in the expansion in part (iii) to estimate the value of $\frac{100}{729}$. [1]

3. i. Find the first three terms in the expansion of $(1 - 2x)^{-\frac{1}{2}}$ in ascending powers of x , where $|x| < \frac{1}{2}$. [3]

- ii. Hence find the coefficient of x^2 in the expansion of $\frac{x+3}{\sqrt{1-2x}}$. [2]

4. i. Find the first three terms in the binomial expansion of $(8 - 9x)^{\frac{2}{3}}$ in ascending powers of x .

[4]

ii. State the set of values of x for which this expansion is valid.

[1]

5. (a) Find the first three terms in the expansion of $(1 + px)^{\frac{1}{3}}$ in ascending powers of x . [3]

(b) Given that the expansion of $(1 + qx)(1 + px)^{\frac{1}{3}}$ is

$$1 + x - \frac{2}{9}x^2 + \dots$$

find the possible values of p and q .

[5]

6. (a) Find the first three terms in the expansion of $(1 + 2x)^{\frac{1}{2}}$ in ascending powers of x . [3]

(b) Obtain an estimate of $\sqrt{3}$ by substituting $x = 0.04$ into your answer to part (a). [3]

(c) Explain why using $x = 1$ in the expansion would not give a valid estimate of $\sqrt{3}$. [1]

7. (i) Find the first three terms in ascending powers of x in the binomial expansion of $\sqrt[4]{1 + 8x}$. [3]

(ii) State the range of values for which this expansion is valid. [1]

8. (a) Find the first three terms in the expansion of $(4 - x)^{-\frac{1}{2}}$ in ascending powers of x . [4]

- (b) $\frac{a+bx}{\sqrt{4-x}}$ [3]
The expansion of $\frac{a+bx}{\sqrt{4-x}}$ is $16 - x \dots$. Find the values of the constants a and b .

9. (a) Find the coefficient of x^4 in the expansion of $(3x-2)^{10}$. [2]

- (b) In the expansion of $(1+2x)^n$, where n is a positive integer, the coefficients of x^7 and x^8 are equal.
Find the value of n . [3]

- (c) Find the coefficient of x^3 in the expansion of $\frac{1}{\sqrt{4+x}}$. [4]

10. (a) Expand $\sqrt{1+2x}$ in ascending powers of x , up to and including the term in x^3 . [4]

- (b) $\frac{\sqrt{1+2x}}{1+9x^2}$ [3]
Hence expand $\frac{\sqrt{1+2x}}{1+9x^2}$ in ascending powers of x , up to and including the term in x^3 .

- (c) Determine the range of values of x for which the expansion in part (b) is valid. [2]

END OF QUESTION paper

Mark scheme

Question	Answer/Indicative content	Marks	Part marks and guidance
1	<p>The first 3 marks refer to the expansion...</p> <p>First 2 terms = $1 - \frac{8}{3}x$</p> <p>3rd term = $\frac{\frac{3}{2} \cdot \frac{1}{2}}{1.2} \left(-\frac{16x}{9}\right)^2$</p> <p>= $\frac{32}{27}x^2$</p> <p>Complete expansions $\approx 27 - 72x + 32x^2$</p> <p>valid for $\frac{-9}{16} < x < \frac{9}{16}$ or $x < \frac{9}{16}$</p>	<p>.....</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p>	<p><u>of</u> $\left(1 - \frac{16x}{9}\right)^{\frac{3}{2}}$ and to no other expansion</p> <p>Allow any equiv fraction for the $-\frac{8}{3}$ and ISW</p> <p>Allow clear evidence of intention, e.g.</p> $\frac{\frac{3}{2} \cdot \frac{1}{2} \cdot -16x^2}{1.2 \cdot 9}$ <p>Allow any equiv fraction for the $\frac{32}{27}$ and ISW</p> <p>cao No equivalents. Ignore any further terms</p> <p>oe Beware, e.g.</p> $x < \left \frac{9}{16} \right $ <p>Examiner's Comments</p> <p>Most candidates were confident with the binomial</p> <p>$\frac{3}{2} - \frac{16}{9}$ is not an equiv fraction</p> <p>If expansion $(a + b)^n$ used, award B1, B1, B1 for 27, - 72x, 32x²</p> <p>condone \leq instead of <</p>

					expansion and were able to change $(9 - 16x)^{\frac{3}{2}}$ into a suitable form for expansion. Common errors in the expansion included careless simplification of the x^2 term (often because of cramped writing) and multiplication of this expansion by 9 instead of by 27. A significant number of candidates completely ignored the request for the validity.
			Total	5	
2	i	$(1-x)^{-3} = 1 + -3 \cdot -x + \frac{-3 \cdot -4}{2} (-x)^2 + \dots$ <p>accept $3x$ for $-3 \cdot -x$ & / or $-x^2$ or $(x)^2$ for $(-x)^2$</p>	M1	As result is given, this expansion must be shown and then simplified. It must not just be stated as $1 + 3x + 6x^2 + \dots$	For alternative methods such as expanding $(1-x)^3$ and multiplying by $x + 3x^2 + 6x^3$ or using long division, consult TL
	i	multiplication by x to produce AG (Answer Given)	A1	Examiner's Comments	
	i			The required relationship had been given so, as with all such similar questions, the solutions were examined closely to see, firstly, if the method of expansion was known and, secondly, how accurately it was carried out. Any slight error in accuracy was penalised.	
	ii	Clear indication that $x = 0.1$ is to be substituted	M1	e.g. $0.1 + 3(0.1)^2 + 6(0.1)^3$ stated	Calculator value \rightarrow M0
	ii	(estimated value is) $0.1 + 3(0.1)^2 + 6(0.1)^3 = 0.136$	A1	Examiner's Comments	(0.13717... is calculator value of $\frac{100}{729}$)
	ii			It was not immediately obvious just what the suitable value of x was, but a fair number obtained $x = 0.1$ and substituted into the given expansion.	

Sight

$$1 - x = x \left(\frac{1}{x} - 1 \right) \text{ or } 1 - x = -x \left(1 - \frac{1}{x} \right) \text{ or}$$

of

$$\left(\frac{1}{x} - 1 \right)^3 = - \left(1 - \frac{1}{x} \right)^3$$

$$\text{or } \left(\frac{1}{x} - 1 \right)^{-3} = - \left(1 - \frac{1}{x} \right)^{-3} \text{ or}$$

$$\left(\frac{1}{x} - 1 \right)^{-3} = - \left(1 - \frac{1}{x} \right)^{-3} \text{ or equivalent}$$

Complete satisfactory explanation (no reference to style) www

$$\left[1 + (-3) \left(-\frac{1}{x} \right) + \frac{(-3)(-4)}{2} \left(-\frac{1}{x} \right)^2 + \dots \right]$$

$$\rightarrow -\frac{1}{x^2} - \frac{3}{x^3} - \frac{6}{x^4}$$

B1

B1

M1

A1

(Answer Given)

Simplified expansion may be quoted - it may have come from result in part (i).

Answer for this expansion is not **AG**.

Examiner's Comments

The required given identity was not difficult to prove, but most made heavy weather of it; simple stages, showing

$$\underline{1}$$

how **x** and the

negative sign were produced, were needed. Whether

					the identity had or had not been proved, it could then be used to produce the required expansion.
		<p>Must say "Not suitable" and one of following:</p> <p>iv $\left \frac{1}{x} \right < 1$ Either: requires $\left \frac{1}{x} \right < 1$</p> <p>which is not true if $x = 0.1$</p> <p>iv Or: substitution of positive / small value of x in the expansion gives a negative / large value (which cannot be an approximation to 100/729).</p> <p>iv</p>	B1	<p>This B1 is dep on $x = 0.1$ used in (ii).</p> <p>Or "because $\frac{1}{x} > 1$"</p> <p>Or "it gives - 63100"</p> <p>Examiner's Comments</p> <p>A simple explanation was required indicating why the value of x used in part (ii) would be unsuitable if used with the expansion in part (iii). Accepted reasons included the fact that -63100 would be the result or that the substitution of a positive/small value of x would give a negative/large value, which could not be an approximation to $\frac{100}{729}$.</p>	<p>Realistic reason</p> <p>If choice given, do not ignore incorrect comments, but ignore irrelevant / unhelpful ones</p>
		Total	9		
3		<p>i $1 + \left(-\frac{1}{2}\right)(-2x) + \left(-\frac{1}{2}\right)\left(\frac{-3}{2}\right)\frac{(\pm 2x)^2}{2!} [+...]$</p> <p>i $1 + x + \frac{3}{2}x^2$ oe</p>	B1	first two terms	allow recovery from omission of brackets
			B1	third term	do not allow $2x^2$ unless fully recovered in answer
			B1		

		ii	use of $(x + 3) \times \text{their} \left(1 + x + \frac{3}{2}x^2\right)$	M1	or B2 www in either part	
		ii	coefficient is 5.5 oe	A1	This was very well done by nearly all candidates. A few candidates made a sign error with the first term, and some omitted "2" in part (i). Most gained at least the method mark in part (ii), although a few tried division instead of multiplication.	may be embedded (eg $5.5x^2$ alone or in expansion)
			Total	5		
4		i	$8^{2/3} = 4$	B1		may be embedded
		i	$\left(1 - \frac{9x}{8}\right)^{2/3}$ seen	M1	$8^{2/3} + \left(\frac{2}{3}\right)8^{-1/3}(\pm 9x)$ $+ \frac{\frac{2}{3} \times \left(\frac{2}{3} - 1\right)}{2!} 8^{-4/3}(\pm 9x)^2$	ignore extra terms
		i	$1 + \left(\frac{2}{3}\right)\left(\frac{\pm 9x}{k}\right) + \frac{1}{2!}\left(\frac{2}{3}\right)\left(\frac{2}{3} - 1\right)\left(\frac{\pm 9x}{k}\right)^2$ where k is an integer greater than 1	M1	$4 + \left(\frac{2}{3}\right)\left(\frac{1}{2}\right)(\pm 9x)$ $+ \frac{\frac{2}{3} \times \left(\frac{2}{3} - 1\right)}{2!} \left(\frac{1}{16}\right)(\pm 9x)^2$	or better
		i	$4 - 3x - \frac{9}{16}x^2$ or $4\left(1 - \frac{3}{4}x - \frac{9}{64}x^2\right)$ <small>cao</small>	A1	This was very well-done, with most candidates scoring at least three out of four marks. A few had difficulty dealing with $8^{2/3}$ and some made sign errors.	

	ii	$-\frac{8}{9} < x < \frac{8}{9} \text{ or } x < \frac{8}{9} \text{ isw}$ cao	B1	<u>Examiner's Comments</u> Many careless slips were seen, such as $x < \frac{8}{9}$ and $ x < -\frac{8}{9}$ but the correct answer was seen in the full range of scripts.	
		Total	5		
5	a	Obtain $1 + \frac{1}{3}px$ $\left(\frac{1}{2}\right)\left(\frac{1}{3}\right)\left(\frac{-2}{3}\right)(px)^2$ Obtain $1 + \frac{1}{3}px - \frac{1}{9}p^2x^2$	B1(AO 1.1) M1(AO1.1) A1(AO1.1) [3]	Must be simplified	Attempt the x^2 term at least in the form ${}^6C_2kx^2$
	b	$(1+qx)\left(1+\frac{1}{3}px-\frac{1}{9}p^2x^2\right)$ $=1+\left(\frac{1}{3}p+q\right)x+\left(\frac{1}{3}pq-\frac{1}{9}p^2\right)x^2$ $\frac{1}{3}p+q=1 \quad (*)$ $\frac{1}{3}pq-\frac{1}{9}p^2=-\frac{2}{9}$ $2p^2-3p-2=0$	M1(AO 3.1a) M1(AO3.1a) M1(AO1.1) A1(AO1.1) A1FT(AO1.1)	Obtain two equations in p and q and show evidence of substitution for p or q to obtain an	Expand $(1+qx)$ and their $1 + \frac{1}{3}px - \frac{1}{9}p^2x^2$ and compare coefficients Or $18q^2 - 27q + 7$

		$p = 2 \text{ or } -\frac{1}{2}$ $q = \frac{1}{3} \text{ or } \frac{7}{6}$	[5]	<p>equation in one variable Solve a 3 term quadratic equation in a single variable.</p> <p>Obtain any two values</p> <p>Obtain all 4 values, or FT their p and (*)</p>	<p>= 0 Solve their quadratic</p> <p>with indication of correct pairings</p>	
		Total	8			
6	a	$1 + x - \frac{1}{2}x^2$	B1(AO1.1) M1(AO1.1a) A1(AO1.1) [3]	<p>Obtain $1 + x$</p> <p>Attempt third term</p> <p>Obtain correct third term</p>	<p>Terms must be simplified for B / A marks</p>	
	b	$\sqrt{1.08} \approx 1 + 0.04 - 0.5 \times 0.04^2$ $\sqrt{0.36 \times 3} \approx 1.0392$	M1(AO2.1) M1(AO3.1a)	<p>Substitute 0.04 throughout</p>	<p>Need $\sqrt{1.08}$ as well</p>	

		$0.6\sqrt{3} \approx 1.0392$ $\sqrt{3} \approx 1.73$	A1(AO1.1) [3]	Rearrange $\sqrt{1.08}$ to $k\sqrt{3}$ Obtain 1.73 or better	Must see method	
	c	Expansion is only valid for $ x < \frac{1}{2}$	E1(AO2.3) [1]	Explanation must be specific		
		Total	7			
7	i	$1 + 2x$ $\left(\frac{1}{4}\right) \times \left(-\frac{3}{4}\right) \times \frac{(8x)^2}{2!}$ oe soi $1 + 2x - 6x^2$ cao	B1 M1 A1 [3]	allow bracket error	if M0 allow SC1 for $1 + 4x - 8x^2$ ignore extra terms	Examiner's Comments This proved accessible to nearly all candidates, with most scoring full marks. A few made arithmetical slips, and a few used the wrong index: -4 and $\frac{1}{2}$ were the usual errors.

		ii	valid for $ x < \frac{1}{8}$ _{oe}	B1 [1]	<p>Examiner's Comments</p> <p>Although largely well done, this did cause some problems. Common mistakes were to omit one tail of the inequality or to write $x < \left \frac{1}{8} \right$.</p> <p>Occasionally $x < 8$ was seen.</p>											
			Total	4												
8		a	$\left(1 - \frac{1}{4}x\right)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2}\right)\left(-\frac{1}{4}x\right) + \left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{1}{4}x\right)^2$ $= 1 + \frac{1}{8}x + \frac{3}{128}x^2$ $(4-x)^{-\frac{1}{2}} = 4^{-\frac{1}{2}}\left(1 - \frac{1}{4}x\right)^{-\frac{1}{2}} = \frac{1}{2}\left(1 - \frac{1}{4}x\right)^{-\frac{1}{2}}$ $(4-x)^{-\frac{1}{2}} = \frac{1}{2} + \frac{1}{16}x + \frac{3}{256}x^2$	<p>B1 (AO 1.1)</p> <p>M1 (AO 1.1a)</p> <p>A1 (AO 1.1)</p> <p>B1ft (AO 1.1)</p>	<table border="1"> <tr> <td>Obtain correct first two terms</td> <td>Allow unsimplified coeffs</td> </tr> <tr> <td>Attempt third term in expansion of $\left(1 - \frac{1}{4}x\right)^{-\frac{1}{2}}$</td> <td>Product of attempt at binomial coefficient and $\left(-\frac{1}{4}x\right)^2$</td> </tr> <tr> <td>Correct third term</td> <td>Allow BOD on missing brackets</td> </tr> <tr> <td>Correct</td> <td>Allow BOD on missing negative sign in third term</td> </tr> <tr> <td></td> <td>Allow unsimplified</td> </tr> </table>	Obtain correct first two terms	Allow unsimplified coeffs	Attempt third term in expansion of $\left(1 - \frac{1}{4}x\right)^{-\frac{1}{2}}$	Product of attempt at binomial coefficient and $\left(-\frac{1}{4}x\right)^2$	Correct third term	Allow BOD on missing brackets	Correct	Allow BOD on missing negative sign in third term		Allow unsimplified	
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				<p>[4]</p>	<table border="1"> <tr> <td>expansion of $(4-x)^{-\frac{1}{2}}$</td> <td> coeffs ft as $\frac{1}{2}$ (their three term expansion) No ISW if expression subsequently spoiled by attempt to simplify eg $\times 256$ </td> </tr> </table>	expansion of $(4-x)^{-\frac{1}{2}}$	coeffs ft as $\frac{1}{2}$ (their three term expansion) No ISW if expression subsequently spoiled by attempt to simplify eg $\times 256$			
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				<p>Examiner's Comments</p> <p>This question was well answered with many fully correct solutions seen. The most successful solutions made effective use of brackets to ensure that the relevant indices were applied to the entire term including the coefficient of x. Showing clear working allowed partial credit to be credited for attempting a valid method should the final answer not be correct.</p>						
		b	$\frac{1}{2} a = 16$ and hence $a = 32$ $2 + \frac{1}{2}b = -1$ OR $\frac{1}{16}a + \frac{1}{2}b = -1$	<p>B1ft (AO 3.1a)</p> <p>M1 (AO 2.2a)</p>	<table border="1"> <tr> <td>Correct value of a</td> <td>ft their first term from (a)</td> </tr> <tr> <td>Attempt equation involving b and a, or their numerical a</td> <td>Must be using two relevant products (and no others) equated to -1 Allow for</td> </tr> </table>	Correct value of a	ft their first term from (a)	Attempt equation involving b and a , or their numerical a	Must be using two relevant products (and no others) equated to -1 Allow for	
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			$b = -6$	A1 (AO 1.1) [3]	<table border="1"> <tr> <td>Solve to obtain $b = -6$</td> <td>attempting equation – do not need to actually attempt solution for M1 Allow BOD if muddle between terms and coefficients A0 for $-6x$ unless subsequently corrected</td> </tr> </table>	Solve to obtain $b = -6$	attempting equation – do not need to actually attempt solution for M1 Allow BOD if muddle between terms and coefficients A0 for $-6x$ unless subsequently corrected	
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			Total	7				
9	a	${}^{10}C_4 \times 3^4 \times (-2)^6$ oe = 1088640		M1 (AO1.1a) A1 (AO1.1) [2]	<table border="1"> <tr> <td>BC</td> <td></td> </tr> </table>	BC		
BC								

Examiner's Comments

This part of the question was also very well answered. Most candidates appreciated the connection with the previous part of the question, and equated coefficients to find the values of a and b . An alternative method was to cross-multiply and then square both sides before equating coefficients, and this was usually equally successful.

		$\frac{n!}{(n-7)!7!}2^7 = \frac{n!}{(n-8)!8!}2^8$ <p>b</p> $8 = (n-7) \times 2$ $n = 11$	<p>M1 (AO3.1a)</p> <p>M1 (AO1.1a)</p> <p>A1 (AO1.1) [3]</p>	<table border="1"> <tr> <td></td> <td></td> </tr> <tr> <td>Correctly obtaining at least two of 8, (n-7) and 2</td> <td></td> </tr> </table>			Correctly obtaining at least two of 8, (n-7) and 2						
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		$\frac{1}{2} \left(1 + \frac{x}{4}\right)^{-0.5}$ <p>c</p> $\frac{1}{2} \times \frac{(-0.5)(-1.5)(-2.5)}{3!} \times \left(\frac{1}{4}\right)^3$ $= -\frac{5}{2048} \text{ or } -0.00244 \text{ (3 sf)}$	<p>M1 (AO1.1a)</p> <p>M1 (AO1.1)</p> <p>A1FT (AO1.1)</p> <p>A1 (AO1.1) [4]</p>	<table border="1"> <tr> <td>M1 for $k\left(1 + \frac{x}{4}\right)^{-0.5}$</td> <td></td> </tr> <tr> <td>M1 for $\frac{1}{2}$</td> <td></td> </tr> <tr> <td>follow through their 'k'</td> <td></td> </tr> <tr> <td>cao BC</td> <td></td> </tr> </table>	M1 for $k\left(1 + \frac{x}{4}\right)^{-0.5}$		M1 for $\frac{1}{2}$		follow through their 'k'		cao BC		
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		Total	9										
10	a	$(1+2x)^{\frac{1}{2}} = 1+x$ <table border="1"> <tr> <td> $+ \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)(2x)^2}{2} + \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)(2x)^3}{6}$ </td> </tr> </table>	$+ \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)(2x)^2}{2} + \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)(2x)^3}{6}$	<p>B1 (AO 1.1)</p> <p>M1 (AO 1.1a)</p> <p>A1(AO 1.1)</p> <p>A1 (AO 1.1) [4]</p>	<table border="1"> <tr> <td>Obtain correct first two terms</td> <td>Must be simplified</td> </tr> <tr> <td>Attempt at least one more term</td> <td></td> </tr> </table>	Obtain correct first two terms	Must be simplified	Attempt at least one more term					
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		$= 1 + x - \frac{1}{2}x^2 + \frac{1}{2}x^3$		<table border="1"> <tr> <td>Obtain correct third term</td> <td rowspan="2">Must be simplified</td> </tr> <tr> <td>Obtain correct fourth term</td> </tr> </table>	Obtain correct third term	Must be simplified	Obtain correct fourth term				
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	b	$(1 + 9x^2)^{-1} = 1 - 9x^2$ $(1 - 9x^2)(1 + x - \frac{1}{2}x^2 + \frac{1}{2}x^3)$ $= 1 + x - \frac{19}{2}x^2 - \frac{17}{2}x^3$	<p>B1 (AO 3.1a) M1 (AO 1.1a) A1FT (AO 1.1)</p> <p>[3]</p>	<table border="1"> <tr> <td>Correct expansion so i</td> <td rowspan="2">FT their (i) – must be 4 terms</td> </tr> <tr> <td>Attempt expansion</td> </tr> <tr> <td>Obtain correct expansion</td> <td></td> </tr> </table>	Correct expansion so i	FT their (i) – must be 4 terms	Attempt expansion	Obtain correct expansion			
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	c	$(1 + 2x)^{\frac{1}{2}} \Rightarrow x < \frac{1}{2}$ $(1 + 9x^2)^{-1} \Rightarrow x < \frac{1}{3}$ <table border="1"> <tr> <td>hence</td> <td>$x < \frac{1}{3}$</td> </tr> </table>	hence	$ x < \frac{1}{3}$	<p>M1 (AO 1.1)</p> <p>A1 (AO 2.3)</p> <p>[2]</p>	<table border="1"> <tr> <td>At least one correct condition seen</td> <td>oe</td> </tr> <tr> <td>Correct conclusion, from both correct conditions</td> <td>oe</td> </tr> </table>	At least one correct condition seen	oe	Correct conclusion, from both correct conditions	oe	
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